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## What does a Computer

## Understands

Computers do not understand natural languages nor programming languages. They only understand the language of bits. A bit is the most basic unit in computer machine language. All instructions that the computer executes and the data that it processes is made up of a group of bits. Bits are represented in many forms either through electrical voltage, current pulses, or by the state of an electronic flip-flop circuit in form of o or 1 .

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## Boolean Logic

Because of computer understands machine language(o/1) which is binary value so every operation is done with the help of these binary value by the computer.
George Boole, Boolean logic is a form of algebra in which all values are reduced to either 1 or 1.
To understand boolean logic properly we have to understand Boolean logic rule,Truth table and logic gates

## Boolean Logic

 rulesBoolean Algebra is the mathematics we use to analyse digital gates and circuits. We can use these "Laws of Boolean" to both reduce and simplify a complex Boolean expression in an attempt to reduce the number

Boolean
Expression

| $\mathrm{A}+1=1$ | Annulment |
| :---: | :---: |
| $\mathbf{A}+\mathbf{o}=\mathbf{A}$ | Identity |
| A. $\mathbf{1}=\mathrm{A}$ | Identity |
| A. $\mathbf{o}=0$ | Annulment |
| $\mathbf{A}+\mathbf{A}=\mathbf{A}$ | Idempotent |
| A. A = A | Idempotent |
| NOT A = A | Double Negation |
| $\mathrm{A}+\mathrm{A}=1$ | Complement |
| A. $\mathrm{A}=0$ | Complement |
| $\mathbf{A}+\mathrm{B}=\mathbf{B}+\mathrm{A}$ | Commutative |
| A.B = B. $A$ | Commutative |
| $\mathbf{A}+\mathbf{B}=\mathbf{A} . \mathrm{B}$ | de Morgan's Theorem |
| $A . B=A+B$ | de Morgan's Theorem |

## Boolean Expression

A Boolean expression is a logical statement that is either TRUE or FALSE .
A Boolean expression can consist of Boolean data, such as the following:

* BOOLEAN values (YES and NO, and their synonyms, ON and OFF, and TRUE and FALSE)
* BOOLEAN variables or formulas
* Functions that yield BOOLEAN results
- BOOLEAN values calculated by comparison operators. E.g.

1. $\$ F(x, y, z)=x^{\prime} y^{\prime} z^{\prime}+x y^{\prime} z+x y z+x y z$
2. $\$ F^{\prime}(x, y, z)=x^{\prime} y z+x^{\prime} y^{\prime} z+x^{\prime} y z^{\prime}+x y^{\prime} z^{\prime}$
3. $\$ F(x, y, z)=(x+y+z) \cdot\left(x+y+z^{\prime}\right) \cdot\left(x+y^{\prime}+z\right) \cdot\left(x^{\prime}+y+z\right)$

## De Morgan's Law

The complement of the union of two sets is equal to the intersection of their complements and the complement of the intersection of two sets is equal to the union of their complements. These are called De Morgan's laws.

For any two finite sets A and B
(i) $(A \cup B)^{\prime}=A^{\prime} \cap B^{\prime}$ (which is a De Morgan's law of union). OR
$(A+B)^{\prime}=A^{\prime} . B^{\prime}$
(ii) $(A \cap B)^{\prime}=A^{\prime} U B^{\prime}$ (which is a De Morgan's law of intersection). OR
$(A . B)^{\prime}=A^{\prime}+B^{\prime}$ isit : python.mykvs.in for regular updates

Proof of De Morgan's law: (A U B)' $=A^{\prime} \cap B^{\prime}$
Let $\mathrm{P}=(\mathrm{A} U \mathrm{~B})^{\prime}$ and $\mathrm{Q}=\mathrm{A}^{\prime} \cap \mathrm{B}^{\prime}$
Let $x$ be an arbitrary element of $P$ then $x \in P \Rightarrow x \in(A \cup B)^{\prime}$
$\Rightarrow \mathrm{x} \notin(\mathrm{A} U \mathrm{~B})$
$\Rightarrow \mathrm{x} \notin \mathrm{A}$ and $\mathrm{x} \notin \mathrm{B}$
$\Rightarrow \mathrm{x} \in \mathrm{A}^{\prime}$ and $\mathrm{x} \in \mathrm{B}^{\prime}$
$\Rightarrow \mathrm{x} \in \mathrm{A}^{\prime} \cap \mathrm{B}^{\prime}$
$\Rightarrow \mathrm{x} \in \mathrm{Q}$
Therefore, $\mathrm{P} \subset \mathrm{Q} . . . . . . . . . . . . . . . . ~(i) ~$
Again, let $y$ be an arbitrary element of $Q$ then $y \in Q \Rightarrow y \in A^{\prime} \cap B^{\prime}$
$\Rightarrow \mathrm{y} \in \mathrm{A}^{\prime}$ and $\mathrm{y} \in \mathrm{B}^{\prime}$
$\Rightarrow y \notin A$ and $y \notin B$
$\Rightarrow \mathrm{y} \notin(\mathrm{A} \cup \mathrm{B})$
$\Rightarrow \mathrm{y} \in(\mathrm{A} \cup B)^{\prime}$
$\Rightarrow \mathrm{y} \in \mathrm{P}$
Therefore, $\mathrm{Q} \subset \mathrm{P}$
Now combine (i) and (ii) we get; $P=Q$ i.e. $(A \cup B)^{\prime}=A^{\prime} \cap B^{\prime}$ Visit : python.mykvs.in for regular updates

Proof of De Morgan's law: $(\mathrm{A} \cap \mathrm{B})^{\prime}=\mathrm{A}^{\prime} \mathrm{U} \mathrm{B}^{\prime}$
Let $\mathrm{M}=(\mathrm{A} \cap \mathrm{B})^{\prime}$ and $\mathrm{N}=\mathrm{A}^{\prime} \mathrm{U} \mathrm{B}^{\prime}$
Let $x$ be an arbitrary element of $M$ then $x \in M \Rightarrow x \in(A \cap B)^{\prime}$
$\Rightarrow \mathrm{x} \notin(\mathrm{A} \cap \mathrm{B})$
$\Rightarrow \mathrm{x} \notin \mathrm{A}$ or $\mathrm{x} \notin \mathrm{B}$
$\Rightarrow \mathrm{x} \in \mathrm{A}^{\prime}$ or $\mathrm{x} \in \mathrm{B}^{\prime}$
$\Rightarrow \mathrm{x} \in \mathrm{A}^{\prime} \mathrm{UB} \mathrm{B}^{\prime}$
$\Rightarrow \mathrm{x} \in \mathrm{N}$
Therefore, $\mathrm{M} \subset \mathrm{N}$
Again, let $y$ be an arbitrary element of $N$ then $y \in N \Rightarrow y \in A^{\prime} U B^{\prime}$
$\Rightarrow y \in A^{\prime}$ or $y \in B^{\prime}$
$\Rightarrow \mathrm{y} \notin \mathrm{A}$ or $\mathrm{y} \notin \mathrm{B}$
$\Rightarrow \mathrm{y} \notin(\mathrm{A} \cap \mathrm{B})$
$\Rightarrow y \in(A \cap B)^{\prime}$
$\Rightarrow \mathrm{y} \in \mathrm{M}$
Therefore, $\mathrm{N} \subset \mathrm{M}$
Now combine (i) and (ii) we get; $M=N$ i.e. $(A \cap B)^{\prime}=A^{\prime} U B^{\prime}$

## Truth table

A truth table is a mathematical table used in logic.
e.g.

| $\mathbf{A}$ | $\mathbf{B}$ | (A and B) | (A or B) | $\boldsymbol{n o t}(\mathbf{A}$ and B) | $\boldsymbol{n o t}(\mathbf{A}$ or B) |
| :--- | :--- | :--- | :--- | :--- | :--- |
| True | True | True | True | False | False |
| True | False | False | True | True | False |
| False | True | False | True | True | False |
| False | False | False | False | True | True |

Visit : python.mykvs.in for regular updates Boolean function. These are used to construct logic circuit.

|  | LOGIC GAIES |  |
| :---: | :---: | :---: |
| Logic gate symbol | Description | Bcolean |
| $-\square$ | The AND gate output is at logic 1 when, and only when all its inputs are at logic 1 . otherwise the output is at logic 0 . | $X=A \cdot B$ |
|  | The OR gate output is at logic $\mathbf{1}$ when one or more of its inputs are at logic 1 . If all the inputs are at logic 0 , the output is at logic 0 . | $X=A+B$ |
|  | The NAND Gate output is at logic 0 when, and only when all its inputs are at logic 1. otherwise the output is at logic $\mathbf{1}$. | $X=\bar{A} \cdot \mathrm{~B}$ |
| $\mathrm{A}-\mathrm{x}$ | The NOR gate output is at logle O when one or more of its inputs are at logle 1. If all the inputs are at logic 0 , the output is at logic 1. | $X=A+B$ |
| $\stackrel{A \rightarrow}{B \rightarrow} \longrightarrow$ | The XOR gate output is at logic 1 when one and ONLY ONE of its inputs is at logic 1. Otherwise the output is logic 0 . | $\mathrm{X}=\mathrm{A} \oplus \mathrm{B}$ |
| $\mathrm{A} \rightarrow D>0-\mathrm{x}$ | The XNOR gate output is at logic 0 when one and ONLY ONE of its inputs is at logic 1. Otherwise the output is logic 1 . (It is similar to the XOR gate, but its output is inverted). | $X=A \oplus B$ |
|  | The NOT gate output is at logic 0 when its only input is at logic 1, and at logic 1 when its only input is at logic O. For this reason it is often called an INVERTER. | $X=\bar{A}$ |
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## Logic circuit

Construct a truth tables for following circuits of logic gates


Construct the logic circuit of following

1. $\mathrm{C}+\mathrm{BC}$ :
2. $\mathrm{AB}+\mathrm{BC}(\mathrm{B}+\mathrm{C})$

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Universal gates are the logic gates which are capable of implementing any Boolean function without requiring any other type of gate.

Types of Universal Gates-
In digital electronics, there are only two universal gates which are-

1. NAND Gate
2. NOR Gate

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